

Serial No. of Q. C. A. B.

Total No. of Questions : 58]

Code No. : 81-E

[ Total No. of Printed Pages : 40

## ఎిజ్ఞయ : గగణిత

Subject : MATHEMATICS
(ఇంగ్లిజ్ భాఱలంతర / English Version )

దినృంశ: 16. 06. 2014]
戸ఎుయు : బిళిగ్గ 9-30 రింద ముధ్యాळ 12-45 రఎరిగి ]
※రమూఎధి అంచేగళు : 100]
[ Date: 16. 06. 2014
[ Time : 9-30 A.M. to 12-45 P.M.
[ Max. Marks : 100

## FOR OFFICE USE ONLY

| Q. <br> No. | Marks |
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| Q. <br> No. | Marks |
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| Total Marks in words |  |  | Grand Total |  |
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| Signature of Evaluators | Registration No. | Signature of the Deputy Chief | Signature Invig | the Room ator |

General Instructions:
i) The Question-cum-Answer Booklet consists of objective and subjective types of questions having 58 questions.
ii) Space has been provided against each objective type question. You have to choose the correct choice and write the complete answer along with its alphabet in the space provided.
iii) For subjective type questions enough space for each question has been provided. You have to answer the questions in the space.
iv) Follow the instructions given against both the objective and subjective types of questions.
v) Candidate should not write the answer with pencil. Answers written in pencil will not be evaluated. (Except Graphs, Diagrams \& Maps )
vi) In case of Multiple Choice, Fill in the blanks and Matching questions, scratching / rewriting / marking is not permitted, thereby rendering to disqualification for evaluation.
vii) Candidates have extra 15 minutes for reading the question paper.
viii) Space for Rough Work has been printed and provided at the bottom of each page.
I. Four alternatives are given for each of the following questions / incomplete statements. Only one of them is correct or most appropriate. Choose the correct alternative and write the complete answer along with its alphabet in the space provided against each question.

1. If matrix $A=\left[\begin{array}{lll}1 & 2 & 3\end{array}\right]$ and $B=\left[\begin{array}{lll}3 & 2 & 1\end{array}\right]$ then the matrix $A B^{1}$ is
(A) $\left[\begin{array}{l}3 \\ 4 \\ 3\end{array}\right]$
(B) $\left[\begin{array}{lll}3 & 4 & 3\end{array}\right]$
(C) $\left[\begin{array}{lll}2 & 4 & 3\end{array}\right]$
(D) $\quad\left[\begin{array}{ll}1 & 0\end{array}\right]$.

Ans.:
2. The value of ${ }^{5} P_{1}$ is
(A) 5
(B) 6
(C) 0
(D) 5 !

Ans. : $\qquad$
3. The meaningful among the following is
(A) ${ }^{2} P_{5}$
(B) ${ }^{5} P_{2}$
(C) ${ }^{-5} P_{2}$
(D) ${ }^{5} P_{-2}$

Ans. : $\qquad$
4. If ${ }^{11} P_{r}=990$, then the value of $r$ is
(A) 3
(B) 9
(C) 4
(D) 2 .

Ans. : $\qquad$
5. The standard deviation and coefficient of variation of the scores of a player are 1.5 and 15 respectively. Then the mean score of the player is
(A) 1.5
(B) 10
(C) 15
(D) 1000 .

Ans. : $\qquad$
6. The L.C.M. of $2 a b$ and $6 a c^{2}$ is $6 a b c^{2}$. Then their HCF is
(A) $2 a$
(B) $6 a b$
(C) $6 a$
(D) $2 a b$.

Ans. : $\qquad$
7. The HCF of $(p-q)$ and $(\sqrt{p}-\sqrt{q})$ is
(A) $\left(\sqrt{p^{3}}-\sqrt{q^{3}}\right)$
(B) $(\sqrt{p}-\sqrt{q})$
(C) $(\sqrt{p}+\sqrt{q})$
(D) $(p-q)$.

Ans. : $\qquad$
8. The simplified form of $\sum_{p q r}(p+q-r)+\sum_{p q r}(p-q-r)$ is
(A) $2 p+2 q+2 r$
(B) $-p-q-r$
(C) 0
(D) $-2 p-2 q-2 r$.

Ans. : $\qquad$
9. If $a b+b c+c a=1$ then $(a+b)(c+a)=$
(A) $a c$
(B) $1+b c$
(C) $b c$
(D) $1+a^{2}$.

Ans. : $\qquad$
10. If $\sum_{a b c} a^{3}-3 a b c=0$ then the value of $\sum_{a b c} a^{2}=$
(A) $\quad \sum_{a b c} a$
(B) $2 \sum_{a b c} a b$
(C) $\sum_{a b c} a^{2}-a$
(D) $\sum_{a b c} a b$.

Ans. : $\qquad$
11. The sum of $4 \sqrt{2}, \sqrt{2}$ and $-\sqrt{32}$ is
(A) $-\sqrt{2}$
(B) $9 \sqrt{2}$
(C) $4 \sqrt{2}$
(D) $\sqrt{2}$.

Ans. : $\qquad$
12. If $F=\frac{m V^{2}}{r}$ then $V=$
(A) $\pm \sqrt{\frac{F}{m \cdot r}}$
(B) $\pm \sqrt{\frac{m}{F \cdot r}}$
(C) $\pm \sqrt{\frac{F \cdot m}{r}}$
(D) $\pm \sqrt{\frac{F \cdot r}{m}}$.

Ans. : $\qquad$
13. The roots of the quadratic equation $x^{2}-5 x-6=0$ are
(A) - 3 and - 2
(B) 3 and 2
(C) 6 and - 1
(D) -6 and 1 .

Ans. : $\qquad$
14. The value of $p$ for the equation $x^{2}-p x+9=0$ to have equal roots is
(A) +6
(B) $\pm 6$
(C) -6
(D) $\pm 13$.

Ans. : $\qquad$
15. The sum of the roots of the quadratic equation $a x^{2}+b x+c=0$ is
(A) $\frac{c}{a}$
(B) $\frac{b}{a}$
(C) $-\frac{b}{a}$
(D) $\frac{a}{c}$.

Ans. : $\qquad$
16. In the given figure, $E F \| C A$ and $F G \| A B$ then $\frac{D E}{E C}=$

(A) $\frac{D G}{G B}$
(B) $\frac{G B}{D G}$
(C) $\frac{A F}{D F}$
(D) $\frac{A B}{A D}$.

Ans. : $\qquad$
17. In $\triangle P Q R, \angle P Q R=90^{\circ}$. The correct relation with respect to $\triangle P Q R$ is

(A) $\quad P R^{2}=P Q^{2}-Q R^{2}$
(B) $P Q^{2}=Q R^{2}-P R^{2}$
(C) $P R^{2}=P Q^{2}+Q R^{2}$
(D) $Q R^{2}=P Q^{2}-P R^{2}$.

Ans. : $\qquad$
18. The distance between the centres of two circles of radii 3.4 cm and 1.8 cm is 3.7 cm . Then the circles are
(A) externally touching circles
(B) internally touching circles
(C) intersecting circles
(D) concentric circles.

Ans. :
19. Three circles with centres $A, B$ and $C$ touch each other as shown in figure. If the radii of these circles are $8 \mathrm{~cm}, 3 \mathrm{~cm}$ and 2 cm respectively, then the perimeter of $\triangle A B C$ is

(A) 26 cm
(B) 16 cm
(C) 18 cm
(D) 14 cm .

Ans. : $\qquad$
20. In the figure $O$ is the centre of the circle. $A T$ and $B T$ are the tangents at points $A$ and $B$ respectively. If $\angle O A B=30^{\circ}$, then the measure of $\angle A T B$ is

(A) $30^{\circ}$
(B) $15^{\circ}$
(C) $60^{\circ}$
(D) $90^{\circ}$.

Ans. : $\qquad$
( SPACE FOR ROUGH WORK )
II. Fill in the blanks with suitable answers : $10 \times 1=10$
21. If $A$ and $B$ are disjoint sets then $n(A \cap B)=$ $\qquad$

Ans. : $\qquad$
22. The formula to find the $n^{\text {th }}$ term of Harmonic progression is $\qquad$
Ans. : $\qquad$
23. $P$ is a matrix of order $2 \times 3$. Then the order of the transposed matrix of $P$ is $\qquad$
Ans. : $\qquad$
24. The HCF of prime expressions is $\qquad$
Ans. : $\qquad$
25. The $\Sigma$ notation form of $x^{2}+y^{2}+z^{2}$ is $\qquad$ .

Ans. : $\qquad$
26. The standard form of an adfected quadratic equation is $\qquad$ . .

Ans. : $\qquad$
27. The angle between the radius and tangent to a circle at the point of contact is equal to $\qquad$
Ans. : $\qquad$
28. A straight line drawn parallel to one side of a triangle divides the other two sides $\qquad$
Ans. : $\qquad$
29. The curved surface area of a cone of radius $r$ and slant height $l$ is $\qquad$
Ans. : $\qquad$
30. The Euler's formula for polyhedral solid is $\qquad$
Ans. : $\qquad$
III. 31. If the universal set
$U=\{1,2,3,4,5,6,7,8,9\}, P=\{2,3,5,7\}$ and $Q=\{1,3,5,7,9\}$ then prove that $(P \cup Q)^{\prime}=P^{\prime} \cap Q^{\prime}$.
32. A florist has certain number of garlands. 110 of them have champak flowers, 50 have jasmine flowers and 30 garlands have both the flowers. Find the total number of garlands with him.
33. In a geometric progression if $S_{\infty}=\frac{2}{3}$ and $a=1$ then find the geometric progression. 2
34. In a geometric progression the 3 rd term is 8 times the 6 th term, and 4 th term is 4 times the 6 th term. Find the common ratio of the geometric progression. 2
35. Find the value of $x$ if $12, \frac{1}{x-1}, 20$ are in Harmonic progression.

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36. If $A=\left[\begin{array}{ll}3 & 4 \\ 5 & 6\end{array}\right]$ and $B=\left[\begin{array}{ll}1 & 2 \\ 7 & 8\end{array}\right]$ then find $A+2 B$. 2
37. If $a+b+c=a b c$ then prove that $1+a^{2}=(1-a b)(1-a c)$.

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16
38. Find the product of $\sqrt[3]{3}$ and $\sqrt[4]{2}$.
39. Rationalise the denominator and simplify :

$$
\frac{\sqrt{5}+\sqrt{3}}{\sqrt{5}-\sqrt{3}}
$$

40. What is a pure quadratic equation ? Give one example.
41. If $m$ and $n$ are the roots of the quadratic equation $x^{2}-3 x+1=0$, then find the value of $\frac{m}{n}+\frac{n}{m}$.
42. Construct Cayley's table on $A=\{2,4,6,8\}$ under $\oplus \bmod 10$.

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43. In a circle of radius 3 cm draw two radii such that the angle between them is $60^{\circ}$. Construct tangents at the ends of the radii.
44. A mansion has 12 cylindrical pillars, each having the circumference 50 cm and height 3.5 m . Find the cost of painting the lateral surface of all pillars at Rs. 150 per sq. m.
45. 21 spheres of equal radii are melted to form a cylinder of radius 14 cm and height 49 cm . Find the radius of sphere.
46. Draw the plan of the field for the following data :
[Scale : $25 \mathrm{~m}=1 \mathrm{~cm}$ ]

|  | To D (in metres ) |  |
| :---: | :---: | :---: |
|  | 100 |  |
| 50 | 75 | 75 to C |
|  | 50 |  |
|  | 25 | 50 to B |
|  | From A |  |

47. In the given network, write the number of regions and number of arcs.

48. Draw the graph for the given matrix :
$\left[\begin{array}{lll}2 & 1 & 0 \\ 1 & 4 & 1 \\ 0 & 1 & 2\end{array}\right]$
IV. 49. A basket contains 3 white and 5 red flowers. 4 flowers are removed from the basket at random.
a) In how many ways can 4 flowers be removed ?
b) Out of 4 flowers, how many of them may contain 2 white flowers ?
49. Find the standard deviation for the following data :

| Scores $(\boldsymbol{x})$ | 32 | 37 | 42 | 47 | 52 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency $(\boldsymbol{f})$ | 2 | 5 | 6 | 5 | 2 |

51. Find the L.C.M. of $a^{3}-3 a^{2}-10 a+24$ and $a^{3}-2 a^{2}-9 a+18$ by division method.
52. The perimeter of a right angled triangle is 30 cm and its hypotenuse is 13 cm . Find the length of other two sides of the triangle. 3

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53. $A B C D$ is a trapezium in which $A B \| C D$ and $B C \perp A B$. If $A B=7.5 \mathrm{~cm}$, $A D=13 \mathrm{~cm}$ and $C D=12.5 \mathrm{~cm}$, find the length of $B C$. 3
54. Prove that the tangents drawn from an external point to a circle are equal.

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V. 55. Three numbers are in arithmetic progression and their sum is 18 and the sum of their squares is 140 . Find the numbers.
56. Construct two direct common tangents to two circles of radii 4 cm and 2 cm such that the distance between their centres is 10 cm . Measure the length of the tangents and write.
57. Prove that the areas of similar triangles are proportional to the squares of their corresponding sides.
58. Solve graphically :

$$
x^{2}-x-2=0
$$

